
Influence of the Magnetic Field on the Diffusion Capacitance of a Serial Vertical Junction Silicon Solar Cell in Frequency Modulation

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Abstract: In this work, a theoretical study of the effect of the magnetic field on the minority charge carrier density and the diffusion capacity of a silicon solar cell with vertical junction in series in dynamic frequency regime, is done. From the relative continuity equation of the minority charge carriers' density we establish the boundary condition at the junction and the base medium. The expression of the density of minority carriers of charges in the base, allows us to determine the capacity of diffusion of the solar cell according to the magnetic field, the frequency of modulation, the wavelength of illumination and a junction recombination velocity. The profile of the diffusion coefficient allowed us to make a choice on the values of the magnetic field. These values of the magnetic field intensity will be fixed throughout this article. Each value of the magnetic field strength corresponds to a well-defined value of the resonance frequency. We obtained two ranges of illumination wavelengths from the minority charge carrier' density profile. The influence of the magnetic field on the diffusion coefficient, of the density of minority charge carriers in short-circuit and open-circuit conditions and of the diffusion capacity, for a specific wavelength, is theoretically studied.

Keywords: Vertical Junction Solar Cell, Frequency Modulation, Cut-off Frequency, Magnetic Field, Wavelength, Diffusion Capacity, Junction Recombination Velocity

1. Introduction

Photovoltaic conversion is carried out by a solar cell whose conversion efficiency depends on the nature of the semiconductor structure, its technique and its manufacturing processes [1]. Several studies have been conducted on conventional monofacial or bifacial solar cells in monocrystalline or polycrystalline silicon with a back surface field (BSF) cells [2-4]. The authors showed that the diffusion capacity decreases with the magnetic field and the doping rate in the base. Solar cells may be vertical parallel [5, 6], or vertical series [7, 8], and under different static [9], transient [10] and frequency dynamic regimes [11]. Thus, such a structure makes it possible to decouple the absorption axes of the photons and to collect carriers, which offers more degrees of freedom for optimization compared to conventional

horizontal junctions. The current in this device is mainly lateral, the mass losses of resistance in the transmitter area and the electrodes are negligible. As a result, this architecture has a high conversion efficiency under a very high flow concentration [12]. A study of the effect of the applied magnetic field on the diffusion capacity of solar cell with vertical junction series under monochromatic illumination in frequency modulation is proposed.

2. Theory

A series vertical junction silicon solar cell of type n^+-p-p^+ [13] under an applied magnetic field, is shown in figure 1.

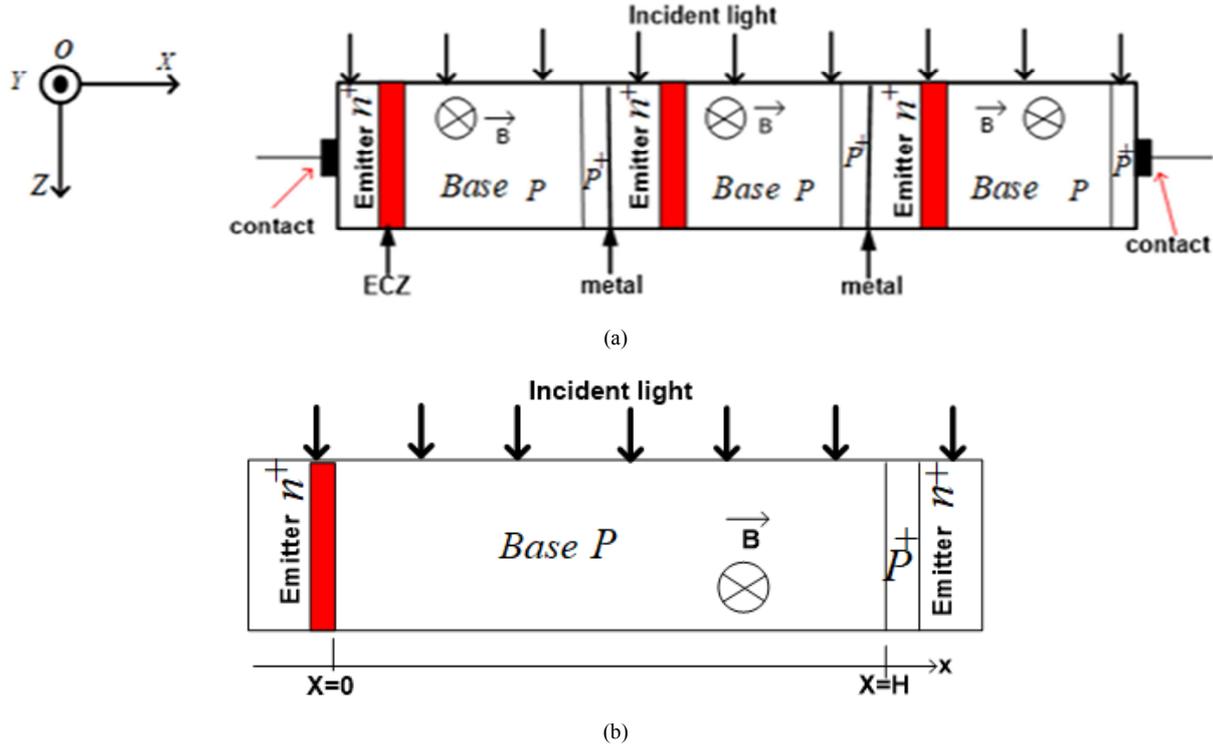


Figure 1. (a) A series vertical junction solar cell with an applied magnetic field, (b) A single structure of a vertical junction solar cell with an applied magnetic field.

H is the total thickness of the base. The magnetic field vector B is perpendicular to the (xoz) plane. When the solar cell is illuminated with light, the photogenerated minority carriers' in the base are governed by the continuity equation [14]:

$$D^* \cdot \frac{\partial^2 \delta(x,z,t)}{\partial x^2} - \frac{\delta(x,z,t)}{\tau} = -G(z,t) + \frac{\partial \delta(x,z,t)}{\partial t} \quad (1)$$

Where x and z , respectively, are variables along x -axis and z -axis; τ is the mean lifetime of the minority carriers; t is the time, $\delta(x,z,t)$ is the minority carriers' density in the base. D^* is the complex diffusion coefficient of the minority carriers in function of the magnetic field and frequency modulation, whose expression is given by [1]:

$$D^* = \frac{D[(1+\tau^2(\omega_r^2+\omega^2))+i\omega\tau(\tau^2(\omega_r^2-\omega^2)-1)]}{(1+\tau^2(\omega_r^2-\omega^2))^2+4\tau^2\omega^2} \quad (2)$$

Where D is the diffusion coefficient of the minority carriers without applied magnetic field [15, 16]; ω_r is the cyclotron angular frequency; ω is the incident angular frequency that is related to the frequency modulation f , by: $\omega = 2\pi f$. The generation rate is given by [17]:

$$G(z,t) = g(z) \cdot e^{i\omega t} \quad (3)$$

With $g(z)$ the spatial component and $e^{i\omega t}$ the temporal component of the generation rate, ω the angular frequency, t the time and i the complex imaginary. The expression of the generation rate $g(z)$ is [18]:

$$g(z) = \phi \cdot \alpha \cdot (1-R)e^{-\alpha z} \quad (4)$$

Where ϕ is the monochromatic incident fluency of light, α the monochromatic absorption coefficient of the material, and R the monochromatic reflection coefficient of the material.

The density of the minority carriers' is given [19]:

$$\delta(x,z,t) = \delta(x,z) \cdot e^{i\omega t} \quad (5)$$

Where $\delta(x,z)$ is the spatial part.

By substituting (3) and (5) in (1), we obtain:

$$\frac{\partial^2 \delta(x,z)}{\partial x^2} - \frac{\delta(x,z)}{L^{*2}} = -\frac{g(z)}{D^*} \quad (6)$$

Where L^* is the complex diffusion length that depends on both magnetic field and frequency modulation. Its expression is:

$$L^{*2} = \tau \cdot D^* \quad (7)$$

A general solution of (6) is given as:

$$\delta(x,z) = K_1 \cdot e^{\frac{x}{L^*}} + K_2 \cdot e^{-\frac{x}{L^*}} + \frac{L^{*2}}{D^*} \cdot \phi \cdot \alpha \cdot (1-R) \cdot e^{-\alpha z} \quad (8)$$

The coefficients K_1 and K_2 can be determined by the following boundaries conditions [11, 20, 21].

1. At the Emitter-base junction ($x = 0$):

$$D^* \cdot \left. \frac{\partial \delta(x,z)}{\partial x} \right|_{x=0} = S_f \cdot \delta(x,z) \Big|_{x=0} \quad (9)$$

2. In the middle of the base ($x = H/2$):

$$\left. \frac{\partial \delta(x,z)}{\partial x} \right|_{x=\frac{H}{2}} = 0 \quad (10)$$

Where S_f is the junction recombination velocity [21, 22] which is related to the photogenerated minority carriers' flux across the junction.

3. Results and Discussions

In this part, the profiles of the diffusion coefficient, the minority carriers' density in the base and the diffusion capacitance are presented.

3.1. Diffusion Coefficient

The profile of the diffusion coefficient according to the logarithm of the angular frequency for different values of the magnetic field, is shown in figure 2.

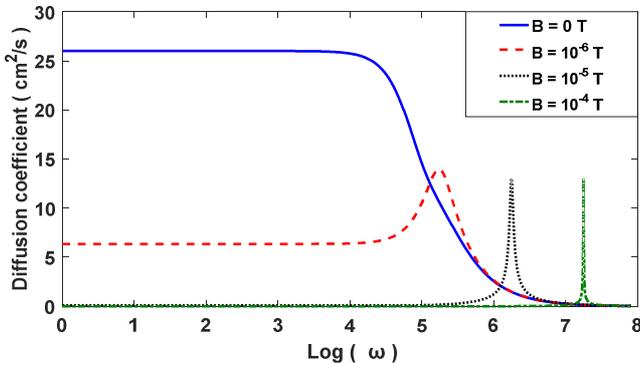


Figure 2. Diffusion coefficient versus the logarithm of the angular frequency for different values of applied magnetic field.

In Figure 2, without an applied magnetic field, the curve of the diffusion coefficient versus the logarithm of the angular frequency shows two zones:

1. the first, in the range [0 rad/s; 10⁴ rad/s] of low angular frequencies values where the diffusion coefficient is constant. It corresponds to the quasi-static regime where there is no delay between the optical excitation of the minority carriers and their response to diffuse in the base;
2. the second, in the range [10⁴ rad/s; 10⁸ rad/s] of relative high angular frequencies values where the diffusion coefficient decreases with the increase of the angular frequency. This zone corresponds to the frequency regime, where there is a phase shift between the optical excitation of the minority carriers and their response.

When an applied magnetic field, the curves of the diffusion coefficient versus the logarithm of the angular frequency, show a few peaks of resonance that are obtained when the modulation frequency is equal to the cyclotron frequency (frequency of the electron in its orbit in the presence of the magnetic field) [23, 24]. This modulation frequency that corresponds to a peak of resonance, is called the resonance angular frequency ω_r . For a given curve, there is a zone corresponding to the quasi-static regime, a resonance zone and a decay zone of the diffusion coefficient. We note that the zone

of the quasi-static regime is being widened from one curve to another when increasing the applied magnetic field. The upper limit value of the angular frequency of the quasi-static regime, are equal to the cut-off frequency ω_c . The amplitude of the diffusion coefficient diminishes with the increase of the magnetic field and this situation implies a degradation of the solar cell properties.

In the table 1, a few values of resonance frequencies and cut-off frequencies are given for different values of the applied magnetic field.

Table 1. A few values of the resonance angular frequency ω_r and cut-off frequency ω_c for different magnetic field values.

Magnetic field B(T)	0	10 ⁻⁶	10 ⁻⁵	10 ⁻⁴
Resonance frequency ω_r (rad/s)	0	1.75.10 ⁵	1.75.10 ⁶	1.75.10 ⁷
Cut-off frequency ω_c (rad/s)	10 ⁴	3.10 ⁴	4.10 ⁵	3.10 ⁶

An increase of the applied magnetic field corresponds also to an increase of the resonance frequency and the cut-off frequency.

3.2. Density of the Minority Carriers

The profile of the minority carriers' density according to the wavelength, for different values of the applied magnetic field, is shown in figure 3.

In Figure 3, the three curves of the minority carriers' density according to the wavelength have the same behavior. In the range of wavelengths [0.3μm; 0.86μm], the density of the minority carriers increases with the wavelength. The absorption of incident photons in the bulk of the base, increases; this leads to an increased photogenerated of the minority carriers. However, in the interval of wavelength [0.86μm; 1.2μm], the density of the minority carriers decreases with the wavelength. The absorption of incident photons in the bulk of the solar cell, decreases: there is a low photogenerated minority carriers. For a wavelength greater than of the threshold wavelength ($\lambda=1.1 \mu\text{m}$), the solar cell becomes transparent and there is any photogenerated minority carriers.

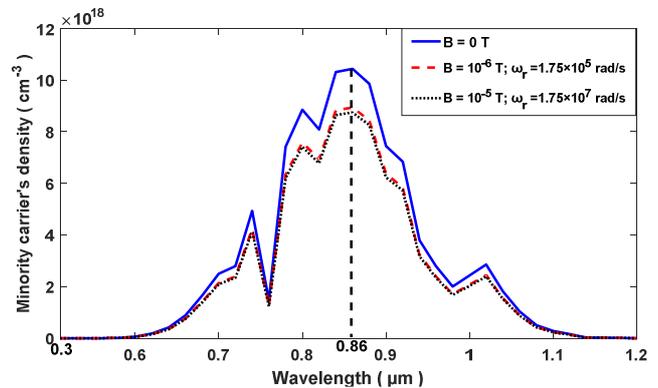


Figure 3. Density of the minority carriers versus the wavelength for different values of the magnetic field. with $z = 0.002 \text{ cm}$.

Without an applied magnetic field ($B = 0\text{T}$), we note that the amplitude of the minority carriers' density is higher than those corresponding to an applied magnetic field. For all three

curves, the density of the minority carriers is maximum at a specific wavelength $\lambda = 0.86 \mu\text{m}$ where the gradient of the density is equal to zero.

In figure 4, the profile of the minority carriers' density according to the base depth, for different values of the magnetic field, in short-circuit situation, is presented.

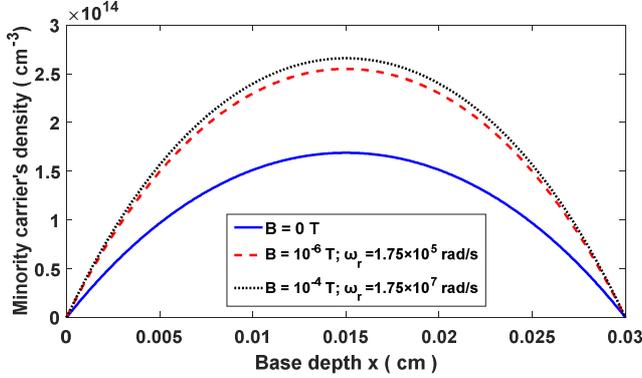


Figure 4. Density of the minority versus the base depth for different values of the applied magnetic field. $z = 0.002 \text{ cm}$; $\lambda = 0.86 \mu\text{m}$; $Sf = 6.10^6 \text{ cm/s}$.

For a given curve, the density of the minority carriers increases with the base depth of the solar cell towards a maximum density that corresponds to the middle of the base thickness at the depth $x = 0.015 \text{ cm}$. Beyond this depth, the density of the minority carriers decreases. We obtain three zones:

1. the first zone, for $0 \leq x < 0.015 \text{ cm}$ the gradient of the minority carriers' density is positive: this fact corresponds to a passage of the photogenerated minority carriers across the junction. The photogenerated minority carriers in the vicinity of the junction have sufficient kinetic energy to cross it in order to produce a photocurrent;
2. the second, at the junction $x = 0.015 \text{ cm}$, the gradient of the minority carriers' density is zero. There is a storage of the photogenerated minority carriers which have not enough kinetic energy to cross the junction;
3. the third, for $0.015 \text{ cm} < x < 0.03 \text{ cm}$, the gradient of the minority carriers' density is positive as the first zone. In this zone, the density of the minority carriers decreases with the increase of the base. The photogenerated minority carriers do not recombine since they have sufficient kinetic energy to cross the junction around the position $x = 0.03 \text{ cm}$.

The density of the minority carriers increases with the applied magnetic field.

An applied magnetic field slows down the diffusion of photogenerated minority carriers and deflects them from their initial trajectories towards the lateral surfaces of the base, while at the position $x = 0.015 \text{ cm}$ there is a storage of photogenerated minority carriers in the base volume of the solar cell.

In Figure 5, the profile of the minority carriers' density according to the base depth for different values of the magnetic field, in open circuit situation, is presented:

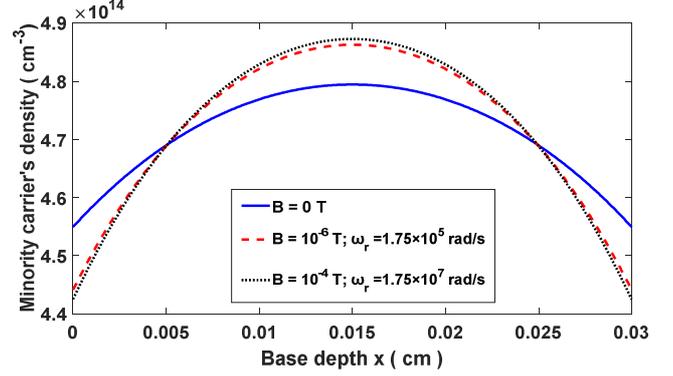


Figure 5. Density of the minority carriers versus the base thickness for different values of the magnetic field. $z = 0.002 \text{ cm}$; $\lambda = 0.86 \mu\text{m}$; $Sf = 2.10^7 \text{ cm/s}$.

In Figure 5, the three curves of the minority carriers' density according to the base depth for different values of the magnetic field, have the same behavior. For a given curve, the minority carriers' density increases with the base depth in the interval $[0 \text{ cm}; 0.015 \text{ cm}]$ [while in the interval $]0.015 \text{ cm}; 0.03 \text{ cm}]$, the minority carriers' density decreases with the base depth. At the depth that corresponds to $x = 0.015 \text{ cm}$, the density of the minority carriers is at its maximum: the gradient of the density at this position is zero and the photogenerated minority carriers are blocked.

When a magnetic field is applied, the three curves of the minority carriers' density are intercepted in two particular positions $x = 0.005 \text{ cm}$ and $x = 0.025 \text{ cm}$ of the base depth. In the interval $[0.005 \text{ cm}; 0.025 \text{ cm}]$, the amplitude of the minority carriers' density increases in the bulk of the base with the increase of the magnetic field. But in the intervals $[0 \text{ cm}; 0.005 \text{ cm}]$ and $[0.025 \text{ cm}; 0.03 \text{ cm}]$, the minority carriers' density decreases with the increase of the magnetic field: here the increase of both the magnetic field and the angular frequency resonance leads to a lower photogenerated minority carriers around the junctions; a part of these photogenerated carriers is recombined at the surface density of states and the others are blocked in the base.

From the position $x = 0 \text{ cm}$ to $x = 0.005 \text{ cm}$ in one hand and $x = 0.025 \text{ cm}$ to $x = 0.03 \text{ cm}$ in the other hand, we obtain a base thickness that is equal to 0.005 cm which delimits the space charge region (SCR) from each of the junctions of the solar cell.

3.3. Diffusion Capacitance

The space charge region of a solar cell can be considered as a plan capacitance [25, 26]. This diffusion capacitance of the solar cell can be resulted to the charge carrier's density variation during their diffusion process in the space charge region [27, 28]. The expression of the diffusion capacitance can be given as [22, 29]:

$$C(Sf, \lambda, \omega, B) = \frac{q \cdot n_i^2}{N_b \cdot V_T} + \frac{q}{V_T} \times \delta(x, z) |_{x=0} \quad (11)$$

Where n_i is the intrinsic concentration of the minority carriers; N_b the doping rate in atoms acceptors in the base; V_T the thermal voltage.

The profile of the diffusion capacitance of the solar cell, for

different values of the magnetic field, according to the junction recombination velocity is presented in figure 6:

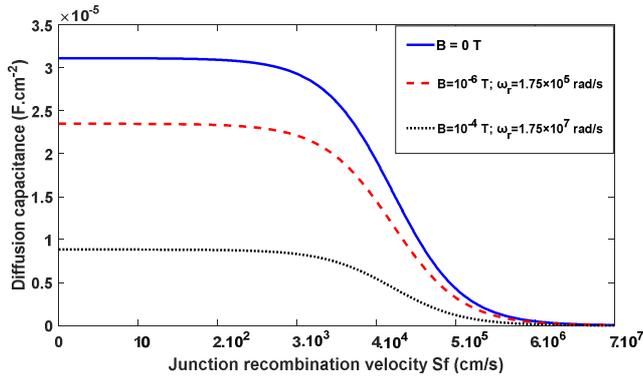


Figure 6. Diffusion capacitance versus junction recombination velocity for different values of the magnetic field $\lambda = 0.86 \mu\text{m}$.

All the three curves that are presented in figure 6, have the same behavior. For a given curve, the diffusion capacitance is constant slightly for a junction recombination velocity lower than $S_f = 3.10^3 \text{ cm/s}$ and its value corresponds to the open-circuit diffusion capacitance C_{co} . For a junction recombination velocity that is upper than $S_f = 3.10^3 \text{ cm/s}$, the diffusion capacitance decreases and tends towards the short circuit diffusion capacitance C_{cc} which can be obtained with $S_f = 6.10^6 \text{ cm/s}$.

The decrease of the diffusion capacitance from the value of C_{co} to the value of C_{cc} , is due both of the space charge zone extension and the lack of blocked photogenerated carriers that have enough kinetic energy to cross the junction. With an applied magnetic field, the amplitude of the diffusion capacitance decreases and the C_{co} and C_{cc} values decrease too.

4. Conclusion

In our study, the effects of the magnetic field, the angular frequency and the wavelength on minority carriers' density, have been presented. The diffusion capacitance of a serial vertical-junction silicon solar cell, is also depicted. The diffusion capacitance decreases with the increase of the magnetic field and the angular frequency while the minority carriers' density increases in a defined intervals of the base depth. The obtained values of the open-circuit diffusion capacitance, are higher than that of the short circuit diffusion capacitance. We noted that the solar cell electrical and diffusion properties are degraded.

We have considered a non-degenerated density of states; in the future, we will take into account of the degenerated density of states and the contribution of the emitter in this study.

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